# **SYLLABUS**

# **GOLAGHAT COMMERCE COLLEGE (AUTONOMOUS)**

# FOUR YEARS UNDER GRADUATE PROGRAMME (FYUGP) [AS PER NEP 2020]



### MATHEMATICAL SCIENCE

[Recommended by B.O.S. in Mathematical Science, Golaghat Commerce College (Autonomous) in its meetings held on 29.11.2024]

Title of the Course	: Classical Algebra and Calculus
Course Code	: MATHMAJ1
Nature of the Course	: MAJOR
<b>Total Credits</b>	: 04 (L=3, T=1, P=0)
Distribution of Marks	: 60 (End Sem) + 40 (In-Sem)

UNITS	CONTENTS	L	Т	Р	Total Hours			
I (11 Marks)	Polar representation of complex number, De Moivre's theorem (both integral and rational index), Roots of complex numbers, nth roots of unity, Application of De Moivre's Theorem, Exponential and logarithmic functions of complex numbers, Hyperbolic functions.	09	03	-	12			
II (16 Marks)	Matrix Algebra, Addition, Transposition, Symmetry, Multiplication of matrices and their properties, Matrix inversion and properties, Systems of linear equations, row reduction and echelon forms, vector equations, rank of a matrix, the matrix equation $Ax=b$ , solution sets of linear systems, applications of linear systems, linear independence. Subspaces of $\mathbb{R}^n$ , dimension of subspaces of $\mathbb{R}^n$	09	03	-	12			
III (11 Marks)	Composite and invertible functions, well ordering property of positive integers, Division algorithm, Divisibility & Euclidean algorithm, Congruence relation between integers, Statement of the Fundamental Theorem of Arithmetic.	09	03	-	12			
IV (11 Marks	Limits and continuity of a function including different approaches, Properties of continuous functions including Intermediate value theorem. Differentiability Higher order derivatives, Leibniz rule and its applications L'Hopitals rule; Applications in business, economics and life sciences.	09	03	-	12			
V (11 Marks)	ReductionFormulaeofthetypes $\int \sin^n x dx$ , $\int \cos^n x dx$ , $\int \tan^n x dx$ , $\int (\log x)^n dx$ and $\int \sin^m x \cos^n x dx$ and their derivations. Rectification, volumeand surface area of revolution of a curve.	09	03	-	12			
	Total	45	15	-	60			
	Where, L: Lectures T: Tutorials P: Practicals							

### MODES OF IN-SEMESTER ASSESSMENT:

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(40 Marks)

20 Marks

20 Marks

- One Internal Examination -
- Others (any two or more)

- o Seminar presentation on any of the relevant topics
- o Assignment
- o Group Discussion
- o Quiz
- o Viva-Voce

# **Text Books:**

- 1. Mappa, S.K., Higher Algebra (Classical), Revised 8th Edition, 2011, Levant Books.
- 2. Meyer, Carl D. (2000). Matrix Analysis and Applied Linear Algebra. Society for Industrial and Applied Mathematics (Siam).
- [3] Anton, Howard, Bivens, Irl, & Davis, Stephen (2013). Calculus (10th ed.). John Wiley & Sons Singapore
- Pte. Ltd. Reprint (2016) by Wiley India Pvt. Ltd. Delhi
- [4] Shanti Narayan and P.K. Mittal, Differential Calculus, S. Chand, 2005
- [5] Shanti Narayan and P.K. Mittal, Integral Calculus, S. Chand, 2007.
- [6] A.R. Vasishtha ; A.K. Vasishtha (1991), Krishna Prakashan Media (P) Ltd. Merrut

# **Reference Books:**

1. Dickson, Leonard Eugene (2009). First Course in The Theory of Equations. The Project Gutenberg eBook (http://www.gutenberg.org/ebooks/29785)

2. Gilbert, William J., & Vanstone, Scott A. (1993). Classical Algebra (3rd ed.). Waterloo Mathematics Foundation, Canada.

- 3. Titu Andreescu and Dorin Andrica, Complex Numbers from A to Z, Birkhauser, 2006.
- 4. Thomas, Jr. George B., Weir, Maurice D., & Hass, Joel (2014). Thomas' Calculus (13<sup>th</sup> ed). Pearson Education, Delhi. Indian Reprint 2017.

Title of the Course	:	Classical Algebra and Calculus
Course Code	:	MATHMIN1
Nature of the Course	:	MINOR
<b>Total Credits</b>	:	04 (L=3, T=1, P=0)
Distribution of Marks	:	60 (End Sem) + 40 (In-Sem)

UNITS	CONTENTS	L	Т	Р	Total Hours
I (11 Marks)	Polar representation of complex number, De Moivre's theorem (both integral and rational index), Roots of complex numbers, nth roots of unity, Application of De Moivre's Theorem, Exponential and logarithmic functions of complex numbers, Hyperbolic functions.	09	03	-	12
II (16 Marks)	Matrix Algebra, Addition, Transposition, Symmetry, Multiplication of matrices and their properties, Matrix inversion and properties, Systems of linear equations, row reduction and echelon forms, vector equations, rank of a matrix, the matrix equation $Ax=b$ , solution sets of linear systems, applications of linear systems, linear independence. Subspaces of $R^n$ , dimension of subspaces of $R^n$	09	03	-	12
III (11 Marks)	Composite and invertible functions, well ordering property of positive integers, Division algorithm, Divisibility & Euclidean algorithm, Congruence relation between integers, Statement of the Fundamental Theorem of Arithmetic.	09	03	-	12
IV (11 Marks	Limits and continuity of a function including different approaches, Properties of continuous functions including Intermediate value theorem. Differentiability Higher order derivatives, Leibniz rule and its applications L'Hopitals rule; Applications in business, economics and life sciences.	09	03	-	12
V (11 Marks)	ReductionFormulaeofthetypes $\int \sin^n x dx$ , $\int \cos^n x dx$ , $\int \tan^n x dx$ , $\int (\log x)^n dx$ and $\int \sin^m x \cos^n x dx$ and their derivations. Rectification, volumeand surface area of revolution of a curve.	09	03	-	12
	Total	45 D. D.	15	-	60
	where, L: Lectures 1: Iutorials I	': Pra	actical	S	

## MODES OF IN-SEMESTER ASSESSMENT:

- One Internal Examination
- Others (any two or more)
  - Seminar presentation on any of the relevant topics
  - o Assignment
  - Group Discussion

(40 Marks)

20 Marks 20 Marks o Quiz

o Viva-Voce

# **Text Books:**

- 1 Mappa, S.K., Higher Algebra (Classical), Revised 8th Edition, 2011, Levant Books.
- 2. Meyer, Carl D. (2000). Matrix Analysis and Applied Linear Algebra. Society for Industrial and Applied Mathematics (Siam).
- Anton, Howard, Bivens, Irl, & Davis, Stephen (2013). Calculus (10th ed.). John Wiley & Sons Singapore Pte. Ltd. Reprint (2016) by Wiley India Pvt. Ltd. Delhi
- 4. Shanti Narayan and P.K. Mittal, Differential Calculus, S. Chand, 2005
- 5. Shanti Narayan and P.K. Mittal, Integral Calculus, S. Chand, 2007.
- 6. A.R. Vasishtha ; A.K. Vasishtha (1991), Krishna Prakashan Media (P) Ltd. Merrut

# **Reference Books:**

1. Dickson, Leonard Eugene (2009). First Course in The Theory of Equations. The Project Gutenberg eBook (http://www.gutenberg.org/ebooks/29785)

- 2. Gilbert, William J., & Vanstone, Scott A. (1993). Classical Algebra (3rd ed.). Waterloo Mathematics Foundation, Canada.
- 3. Titu Andreescu and Dorin Andrica, Complex Numbers from A to Z, Birkhauser, 2006.

4. Thomas, Jr. George B., Weir, Maurice D., & Hass, Joel (2014). Thomas' Calculus (13<sup>th</sup> ed). Pearson Education, Delhi. Indian Reprint 2017.

## Title of the Course: Statistical Method -1 Code: MATHGEC1 Nature of the Course: Generic Elective Total Credits: 03 Distribution of Marks: 45 (35T + 10P) (End Sem) + 30 (In-Sem)

UNITS	CONTENTS	L	Т	Р	Total Hours
I (8 Marks)	<ul> <li>Basic Statistics: Definition and scope of Statistics, Limitations of Statistics, concepts of statistical population and sample.</li> <li>Statistical investigation and Types of Data: Planning and execution stages, quantitative and qualitative data, primary and secondary data, Schedules and Questionnaire, Census Vs Sampling and their merits and demerits.</li> <li>Tabulation and Presentation of Data: Tabulation and graphical representation ( Pie Chart, Histogram, Frequency Polygon, Frequency Curve, Ogives)</li> </ul>	05	01	-	06
II ( 10 Marks)	Measures of Central Tendency: Mathematical averages including arithmetic mean, geometric mean, harmonic mean, Properties and applications. Positional averages: Median, Mode (other partition values including quartiles, deciles and percentiles)	08	02	_	10
III (10 Marks)	<b>Measures of Dispersion:</b> Range, quartile deviation, mean deviation, standard deviation, Properties of standard deviation/ variance, coefficient of variation.	07	02		09
IV (7 Marks)	Simple Correlation and Regression Analysis: Correlation Analysis: Meaning of Correlation: simple, multiple, partial, linear, non-linear, scatter diagram, interpretation of r and rank correlation. <b>Regression analysis:</b> Simple linear regression, Principles of least squares and regression lines, Regression equations and estimation, properties of regression coefficients, Relation between correlation and regression.	08	02		10
V (10 Marks)	<ul> <li>List of Practical: (both calculator and computer based)</li> <li>1. Graphical representation of data.</li> <li>2. Problems on measures of central tendency.</li> <li>3. Problems based on measures of dispersion.</li> <li>4. Problems based on combined mean</li> </ul>			05	10

Where,	L: Lectures	T: Tutorials		P	: Practica
Total		28	7	5	45
and variance 5. Karl Pearson 6. Spearman ran 7.Problems based o	and coefficient of varia correlation coefficient. k correlation on Fitting of Regression	tion. 1 lines.			

#### MODES OF IN-SEMESTER ASSESSMENT:

- One Internal Examination
- Others (any two or more)
  - o Seminar presentation on any of the relevant topics
  - Assignment
  - Group Discussion
  - o Quiz
  - o Viva-Voce

# SUGGESTED READINGS:

1. Goon A.M., Gupta M.K. and Dasgupta B. (2002): Fundamentals of Statistics, Vol. I & II, 8<sup>th</sup> Edition. The World Press, Kolkata.

(30 Marks)

- 2. Miller, Irwin and Miller, Marylees (2006): John E. Freund's Mathematical Statistics with Applications, (7<sup>th</sup> Edition), Pearson Education, Asia.
- 3. Mood, A.M. Graybill, F.A. and Boes, D.C. (2007): Introduction to the Theory of Statistics, 3<sup>rd</sup> Edition, (Reprint), Tata McGraw-Hill Pub. Co. Ltd.
- 4. Barman. M. P., Hazarika. J, Bora. T (2021): Statistical Methods, Mahaveer Pub, Dibrugarh.
- 5. Elhance, D. N., Elhance, V., and Aggarwal, B. M. (1958). Fundamentals of Statistics, Allahabad. Kitab Mahal.
- 6. S.C. Gupta, V.K. Kapoor (2017): Fundamentals of Mathematical Statistics, Sultan Chand & Sons, New Delhi.
- 7. J. Medhi (2024): Statistical Methods: An Introductory Text, New Age International Publisher.

Title of the Course	:	Mathematical Aptitude and Reasoning -I
Nature of the Course	:	Skill Enhancement Course
<b>Total Credits</b>	:	03 (L=2, T=1, P=0)
<b>Distribution of Marks</b>	:	45 (End Sem) + 30 (In-Sem)

Course Description:

The course on Aptitude and Reasoning aims to provide students with a solid foundation of Mathematical and Logical Reasoning and to acquaint them with frequently asked patterns in quantitative aptitude and logical reasoning.

## **Course Objectives:**

- Understand the basic concepts of quantitative ability
- Understand the basic concepts of logical reasoning Skills
- Acquire satisfactory competency in use of reasoning
- To develop the ability to apply logical reasoning to solve complex problems in mathematics and computer science, enhancing their analytical and critical thinking skills through exercises and real-world applications.
- To be proficient in formal logical reasoning and prepared to engage in further study or professional work that involves mathematical logic.

UNITS	CONTENTS	L	Т	Р	Total Hour s
I (15 Marks)	Analogy, Classification, Logical Alphabet and Number sequence, Coding Decoding, Series, Logical arrangement of words, Logical Number, Letter and Symbol series, Logical Matching, Missing Numbers, Odd Man out in series, Mathematical Operation, Blood Relations. Clock, Calendar, Sitting arrangement	12	02	-	10
II (10 Marks)	Sets, subsets, Set operations and the laws of set theory and Venn diagrams. Examples of finite and infinite sets. Standard set operations. Classes of sets. Power set of a set.	08	01	-	10
III (10 Marks)	Number system, Factors and Multiples, LCM and HCF, average, Fraction, Decimal, Percentage, profit and Loss, ratio and Proportion	10	01	-	10
IV (10 Marks)	Data Interpretation: Data Interpretation, Tables, Column Graphs, Bar Graphs, Line Charts, Pie Chart	10	01		
	Total	40	05	-	45

Where, L: Lectures T: Tutorials

#### MODES OF IN-SEMESTER ASSESSMENT:

(30 Marks)

- One Internal Examination
- Others (any two or more)
  - Seminar presentation on any of the relevant topics
  - o Assignment
  - Group Discussion
  - o Quiz
  - Viva-Voce

### **Reference Books:**

- 1. A Modern Approach To Verbal & Non Verbal Reasoning By R S Agarwal
- 2. Analytical and Logical reasoning By Sijwali B S
- 3. Quantitative aptitude for Competitive examination By R S Agarwal
- 4. Quantitative Aptitude by Competitive Examinations by Abhijit Guha 4th edition

:	<b>Real Analysis and Differential Equations</b>
:	MATHMAJ2
:	MAJOR
:	04 (L=3, T=1, P=0)
:	60 (End Sem) + 40 (In-Sem)
	: : : :

UNITS	CONTENTS	L	Т	Р	Total Hours
	(A) Real Analysis				
I (10 Marks)	Algebraic and order properties of R, absolute value and real line, bounded sets, supremum and infimum, completeness property of R, the Archimedean property, the density theorem, intervals, nested interval theorem, uncountability of R.	10	03	_	13
II (10 Marks)	Real sequences, limit of a sequence, convergent sequence, bounded sequence, limit theorems, monotone sequences, monotone convergence theorem, subsequences, monotone subsequence theorem, Bolzano Weierstrass theorem for sequences, Cauchy sequences, Cauchy's convergence criterion, properties of divergence sequences.	10	03	-	13
III (10 Marks)	Infinite series, convergence and divergence of infinite series, Cauchy criterion, Tests for convergence: comparison test, limit comparison test, ratio test, root test, integral test, Raabes's test, Absolute convergence, rearrangement theorem, alternating series, Leibniz test, conditional (non- absolute) convergence.	06	03		09
	(B) Differential Equations				
III (11 Marks)	Concepts and definition of General, particular, explicit, implicit and singular solutions of a differential equation. Exact differential equations and integrating factors, separable equations and equations reducible to this form, linear equation and Bernoulli equations, special integrating factors and transformations.	09	03	-	12
IV (19 Marks)	General solution of homogeneous equation of second order, principle of super position for homogeneous equation, Wronskian: its properties and applications, Linear homogeneous and non-homogeneous equations of higher order with constant coefficients, Euler's equation, method of undetermined coefficients, method of variation of parameters.	10	03	-	13
	Total	45	15	-	60

Where, L: Lectures

#### MODES OF IN-SEMESTER ASSESSMENT: (40 Marks)

- One Internal Examination 20 Marks
- Others (any two or more)

20 Marks

• Seminar presentation on any of the relevant topics

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- o Assignment
- o Group Discussion
- o Quiz
- o Viva-Voce

#### **TEXTBOOKS:**

- 1. Bartle R.G. & Sherbert D.R., Introduction to Real Analysis, 3rd Ed., John Wiley and Sons(Asia) Pvt. Ltd., Singapore,2002.
- 2. Kumar A.& Kumarasen S., A Basic Course in Real Analysis, CRC Press, Reprint 2021.
- 3. Ross S.L., Differential Equations, 3<sup>rd</sup>Ed., John Wiley and Sons, India, 2004.
- 4. Kreyszig, Erwin (2011). Advanced Engineering Mathematics(10th ed.).John Wiley & Sons, Inc. Wiley India Edition 2015.

Title of the Course	:	<b>Real Analysis and Differential Equations</b>
Code	:	MATHMIN2
Nature of the Course	:	MINOR
<b>Total Credits</b>	:	04 (L=3, T=1, P=0)
<b>Distribution of Marks</b>	:	60 (End Sem) + 40 (In-Sem)

UNITS	CONTENTS	L	Т	Р	Total Hours
	(A) Real Analysis				
I (10 Marks)	Algebraic and order properties of R, absolute value and real line, bounded sets, supremum and infimum, completeness property of R, the Archimedean property, the density theorem, intervals, nested interval theorem, uncountability of R.	10	03	-	13
II (10 Marks)	Real sequences, limit of a sequence, convergent sequence, bounded sequence, limit theorems, monotone sequences, monotone convergence theorem, subsequences, monotone subsequence theorem, Bolzano Weierstrass theorem for sequences, Cauchy sequences, Cauchy's convergence criterion, properties of divergence sequences.	10	03	-	13
III (10 Marks)	Infinite series, convergence and divergence of infinite series, Cauchy criterion, Tests for convergence: comparison test, limit comparison test, ratio test, root test, integral test, Raabes's test, Absolute convergence, rearrangement theorem, alternating series, Leibniz test, conditional (non- absolute) convergence.	06	03		09
	(B) Differential Equations				
III (11 Marks)	Concepts and definition of General, particular, explicit, implicit and singular solutions of a differential equation. Exact differential equations and integrating factors, separable equations and equations reducible to this form, linear equation and Bernoulli equations, special integrating factors and transformations.	09	03	-	12
IV (19 Marks)	General solution of homogeneous equation of second order, principle of super position for homogeneous equation, Wronskian: its properties and applications, Linear homogeneous and non-homogeneous equations of higher order with constant coefficients, Euler's equation, method of undetermined coefficients, method of variation of parameters.	10	03	-	13
	Total	45	15	-	60

L: Lectures

**P: Practicals** 

#### MODES OF IN-SEMESTER ASSESSMENT:

• One Internal Examination - (20 Marks)

(40 Marks)

- Others (any two or more) (20 Marks)
  - Seminar presentation on any of the relevant topics
  - Assignment
  - Group Discussion
  - o Quiz
  - o Viva-Voce

#### **Textbooks:**

- Bartle R.G. & Sherbert D.R., Introduction to Real Analysis, 3rd Ed., John Wiley and Sons(Asia) Pvt. Ltd., Singapore,2002.
- 2. Kumar A.& Kumarasen S., A Basic Course in Real Analysis, CRC Press, Reprint 2021.
- 3. Ross S.L., Differential Equations, 3<sup>rd</sup>Ed., John Wiley and Sons, India, 2004.
- 4. Kreyszig, Erwin (2011). Advanced Engineering Mathematics(10th ed.).John Wiley & Sons, Inc. Wiley India Edition 2015.

# Title of the Course: Business Mathematics -II Code: MATHGEC2 Nature of the Course: Generic Elective Total Credits: 03 Distribution of Marks: 45 (35T + 10P) (End Sem) + 30 (In-Sem)

UNITS	CONTENTS	L	Т	Р	Total Hours		
I (8 Marks)	Sets and Logic Sets, subsets, types of set, operations on sets, Classes of sets Cartesian product, Venn diagram, Power of a set, difference and symmetric difference of two sets, Set identities Statements, truth values and truth table, negation, conjunction and disjunction, Statements with quantifiers, compound statements.	05	03	-	8		
II (10 Marks)	<b>Relation and Functions</b> Relation and functions, types of relation, Equivalence relation with examples. Functions, types of functions. graphs of functions, compositions of functions and invertible function.	08	03	-	11		
III (10 Marks)	Matrices and Determinants				08		
	Algebra of Matrices, Matrix Operations, Determinant of a square Matrix, Evaluation of determinants upto order 3 (properties of determinants to be excluded), Adjoint of a Matrix, inverse of a matrix, Solution of system of linear equations (having unique solution and involving not more than 3 variables) using matrix inversion method and Cramer's rule						
IV (7 Marks)	Probability	05	03		08		
(********	Introduction, random experiments, sample space, events and algebra of events. Definitions of Probability – classical, statistical, and axiomatic. Conditional Probability. Baye's Theorem						
V (10 Maarlar)	List of Practical:			05	10		
(10 Marks)	(both calculator and computer based)						
	<ol> <li>Problem based on Venn-Diagram</li> <li>Problem based on Cramer's Rule and matrix method</li> </ol>						
	3. Problem based on Conditional Probability						
	4. Graph of a function	<u> </u>	00	05	15		
	1 0tai	20	09	05	45		
Where, L: Lectures T: Tutorials		P: Practical					

#### MODES OF IN-SEMESTER ASSESSMENT:

#### (30 Marks)

- One Internal Examination
- Others (any two or more)
  - Seminar presentation on any of the relevant topics
  - Assignment
    - Group Discussion
    - o Quiz
    - o Viva-Voce

#### **SUGGESTED READINGS:**

1. Hogg, R.V., Tanis, E.A. and Rao J.M. (2009): Probability and Statistical Inference, 17<sup>th</sup>edition, Pearson Education, New Delhi.

2. Ross, S. M. (2014). Introduction to probability models. Academic Press Inc.

3. Johnson, R. A., Miller, I., and Freund, J. E. (2000). Probability and statistics for engineers.6<sup>th</sup> Edition, Pearson Education India.

4. Rohatgi, V. K., Saleh, A. K. M. E. (2011). An Introduction to Probability and Statistics, Germany, Wiley.

5. Kumar A., Kumaresan S., &Sarma, B.K., A Foundation Course in Mathematics, Narosa Publishing House, 2018.

6. Stewart I., Tall D., The Foundations of Mathematics. Oxford University Press, 2<sup>nd</sup> Ed., 2015.

7. Vohra N.D., Business Mathematics and Statistics, McGraw Hill Education (India) Pvt. Ltd, 2012.

8. Singh J. K., Business Mathematics, Himalaya Publishing House, 2021.

### FOUR YEARS UNDER GRADUATE PROGRAMME IN MATHEMATICAL SCIENCE

### DETAILED SYLLABUS OF 2<sup>nd</sup> SEMESTER

Title of the Course		Mathematical Aptitude and Reasoning -II					
Nature of the Course		Skill Enhancement Course					
Total Credits	:	03 (L=2, T=1, P=0)					
Distribution of Marks		45 (End Sem) + 30 (In-Sem)					
			-	T			

UNITS	CONTENTS	L	Т	Р	Hour s
I (15 Marks)	Direction and distance, Sitting Arrangement, Decision making, Completion of series, Completion of figures, Cubes, Dice, Formation of figures, Mirror image, Water Image, Statement and Arguments	12	02	-	10
II (10 Marks)	Time, Speed and Distance problem, Problems on Age, Time, Work and Wage, Boat and Stream, Perimeter, Surface Area, Volume of Solid, Mixtures and Allegation, Simple Interest and Compound Interest	08	01	-	10
III (10 Marks)	Quadratic Equation, Surds and Indices, logarithm, Functions and Graphs	10	01	_	10
IV (10 Marks)	Measures of Central Tendency : Arithmetic Mean, Median, Mode, Quartiles, Deciles, Percentiles, Graphical method for determination of Median and Mode, Probability- Classical Definition of Probability, Empirical Definition of Probability, Axiomatic definition of Probability.	10	01		
	Total	40	05	-	45

Where, L: Lectures T: Tutorials

P: Practicals

\_ Total

MODES OF IN-SEMESTER ASSESSMENT:

(30 Marks)

- One Internal Examination
- Others (any two or more)
  - Seminar presentation on any of the relevant topics
  - o Assignment
  - Group Discussion
  - o Quiz
  - o Viva-Voce

### **Reference Books:**

1. A Modern Approach To Verbal & Non Verbal Reasoning By R S Agarwal

2. Analytical and Logical reasoning By Sijwali B S

3. Quantitative aptitude for Competitive examination By R S Agarwal

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